

# STAR EbyE Fluctuations

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STAR Collaboration  
QM2001

# EbyE Fluctuations - Outline

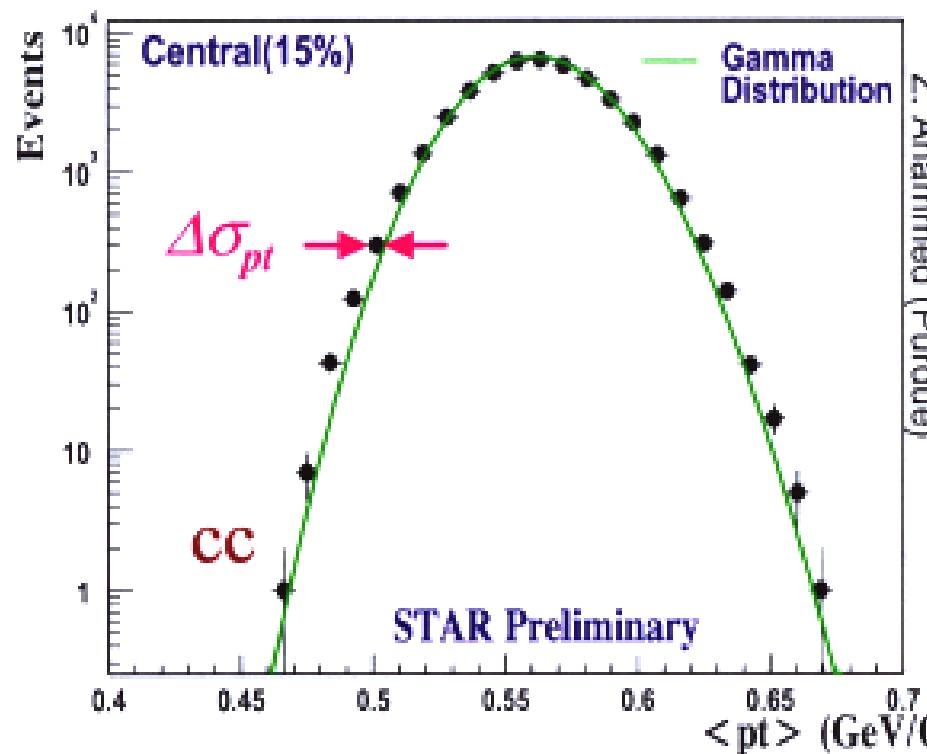
Fluctuation & correlation studies in *transverse* phase space

- Fluctuation measures, two-point correlations and references
- Physics Topics
  - $\langle p_t \rangle$  fluctuations
  - $m_t \times m_t$  correlations
  - $N_+, N_-$  fluctuations
- Fluctuation summary

# Fluctuations, Correlations and References

- Fluctuations
  - variances and covariances
  - covariance matrix
- Correlations
  - two-point densities
  - same/mixed-event pair-density *ratios*
- Fluctuation-Correlation Connection
  - Variance comparisons and *net* two-point correlations are closely related
- Precision references are a key element of correlation analysis in heavy-ion collisions

# $\langle p_t \rangle$ Fluctuations - Distribution

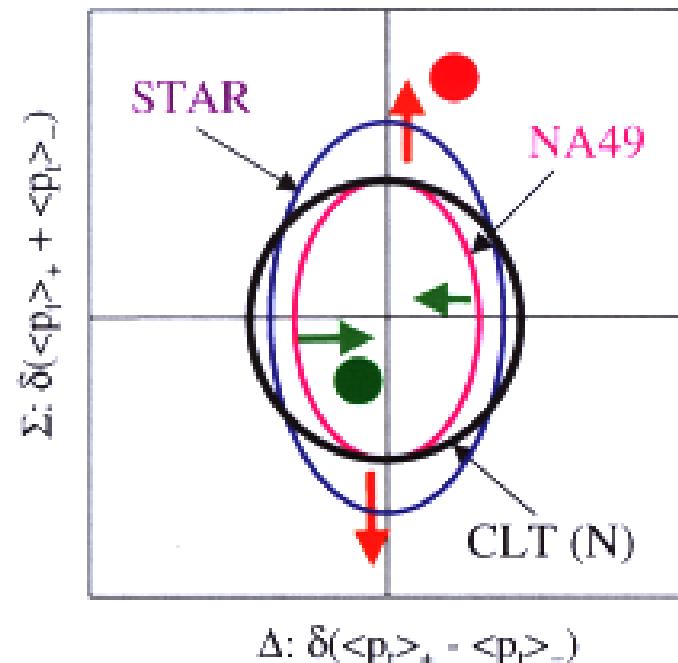
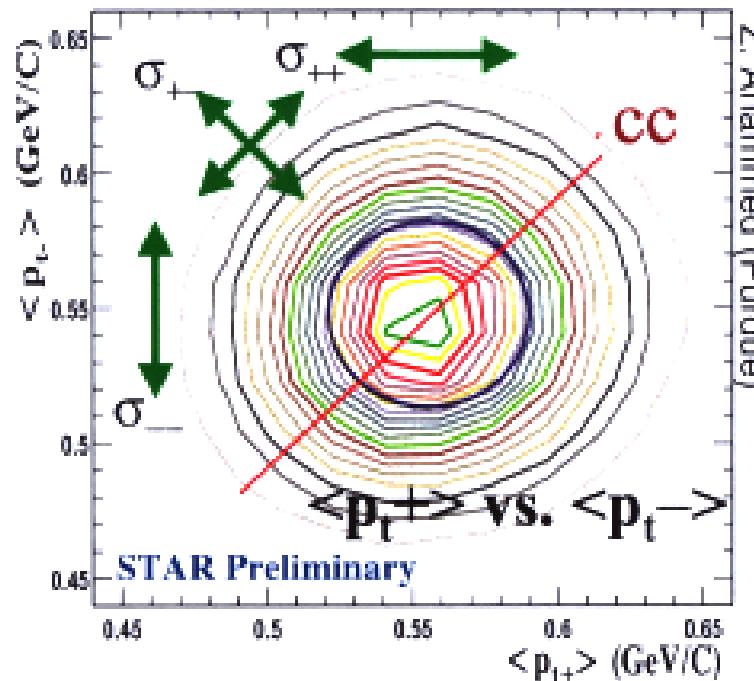


- $\langle p_t \rangle$  distribution compared graphically with gamma-distribution\* inclusive reference
- $\langle p_t \rangle$  variance compared numerically with Central Limit Theorem (CLT) inclusive reference: difference factors  $\Delta\sigma_{pt}$
- STAR data compared to gamma distribution or CLT indicate substantial fluctuation excess ( $\Delta\sigma_{pt} \sim 35$  MeV/c)

$$\overline{N}\sigma_{\langle p_t \rangle}^2 - \sigma_{p_t}^2 \approx 2\sigma_{p_t}(\sqrt{\overline{N}}\sigma_{\langle p_t \rangle} - \sigma_{p_t}) \equiv 2\sigma_{p_t}\Delta\sigma_{p_t}$$

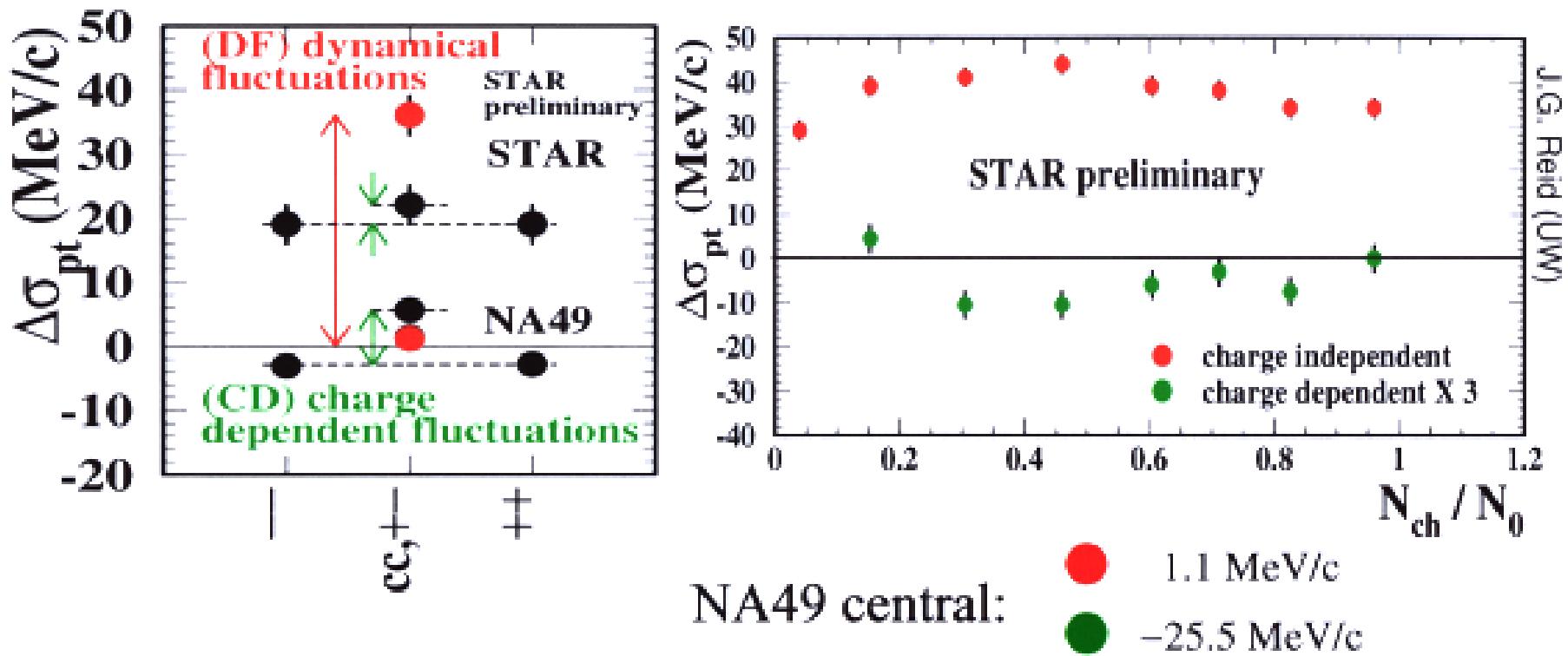
\* M.J. Tannenbaum, QM2001, poster session B; P107

# $\langle p_t \rangle$ Fluctuations - DF and CD



- Difference factor ( $\Sigma$ ) measures **dynamical or charge-independent fluctuations**
  - $N\Delta\sigma_{\Sigma}^2 = N_+\Delta\sigma_{p_t+}^2 + N_-\Delta\sigma_{p_t-}^2 + 2\sqrt{N_+N_-}\Delta\sigma_{p_t+p_t-}^2$
- Difference factor ( $\Delta$ ) between charge-pair types measure **charge-dependent fluctuations**
  - $N\Delta\sigma_{\Delta}^2 = N_+\Delta\sigma_{p_t+}^2 + N_-\Delta\sigma_{p_t-}^2 - 2\sqrt{N_+N_-}\Delta\sigma_{p_t+p_t-}^2$

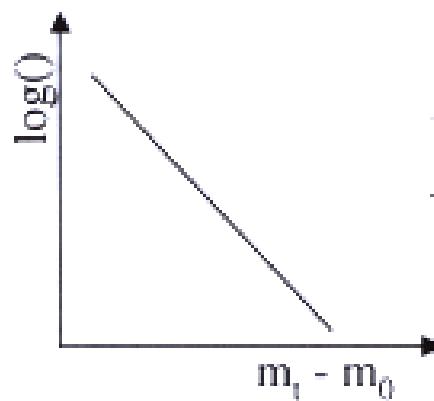
# $\langle p_t \rangle$ Fluctuations - Centrality Dependence



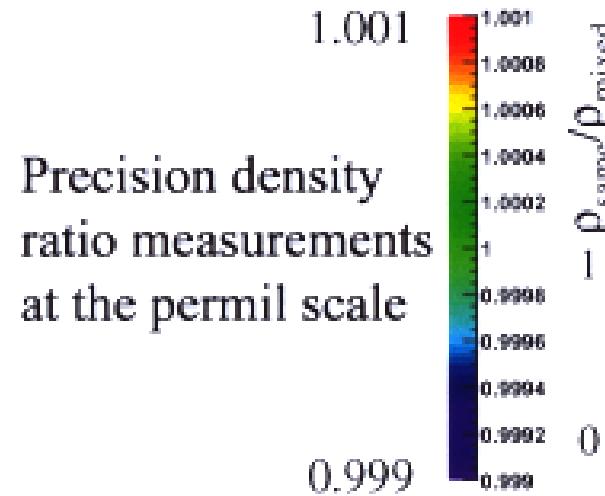
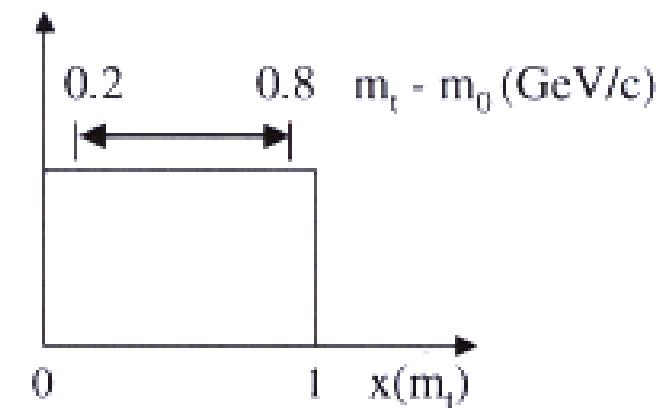
- STAR vs. NA49 differences
  - Rapidity: STAR ( $|\eta| < 1.0$ ) vs NA49 ( $4 < y_\pi < 5.5$ )
  - Multiplicity: STAR (525) vs NA49 (270)
  - see NA49 poster, session A:P082

# $m_t \times m_t$ Correlations - Introduction

M-B distribution



flattening  
transformation

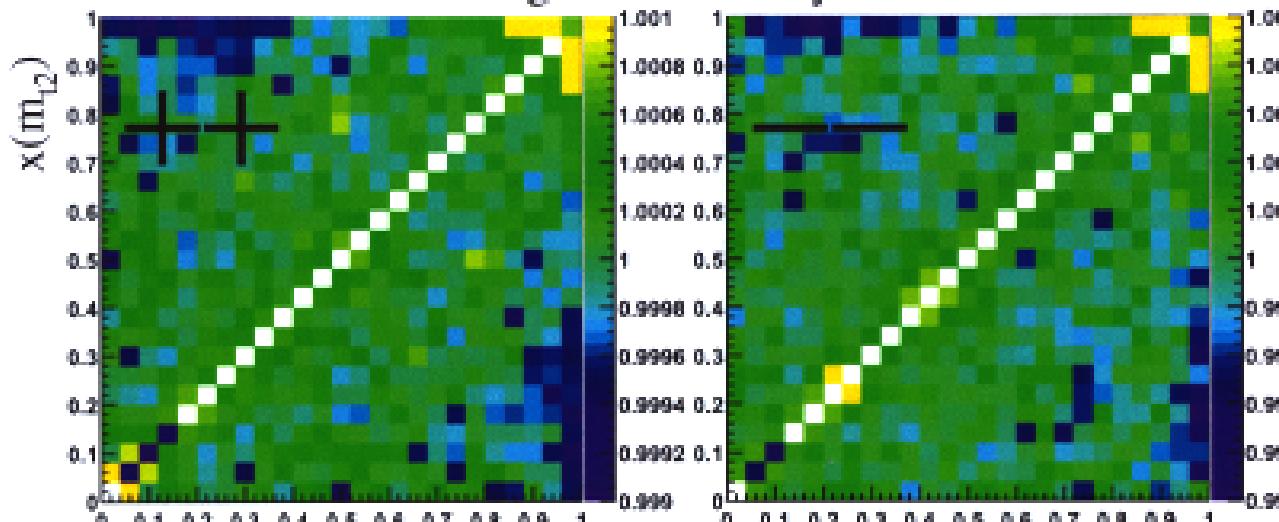


Precision density  
ratio measurements  
at the permil scale

two-point  
density ratio:  
same/mixed-  
pair densities

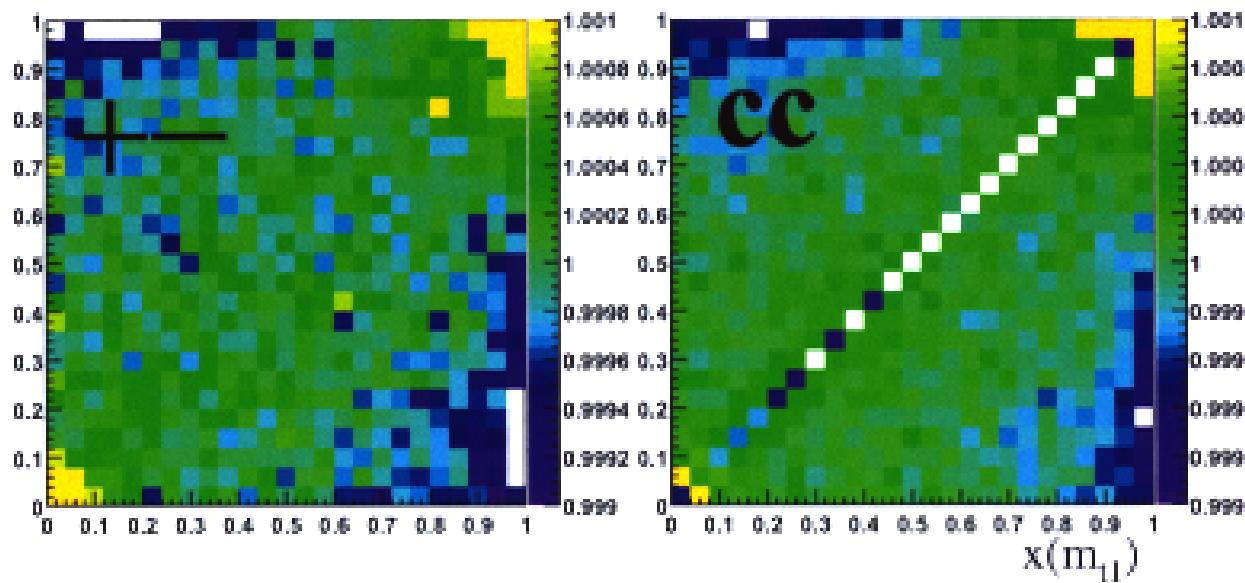
# $m_t \times m_t$ Correlations - Charge Pairs

sibling/mixed density ratios



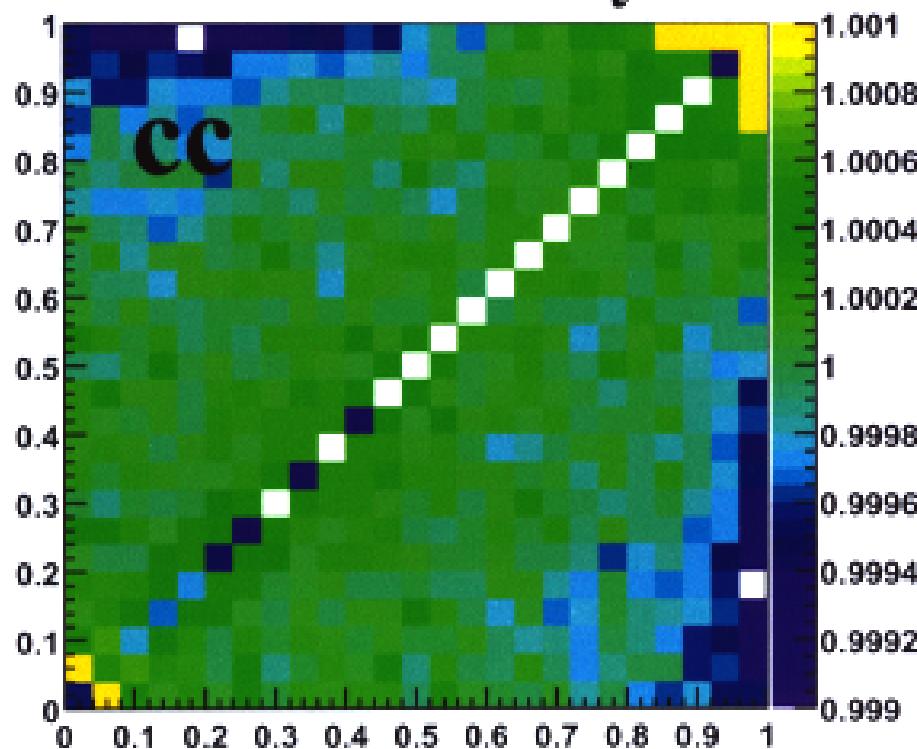
A. Ishihara (UTA), J. Seger (Creighton), J.G. Reid, Q.J. Liu (UW)

STAR Preliminary

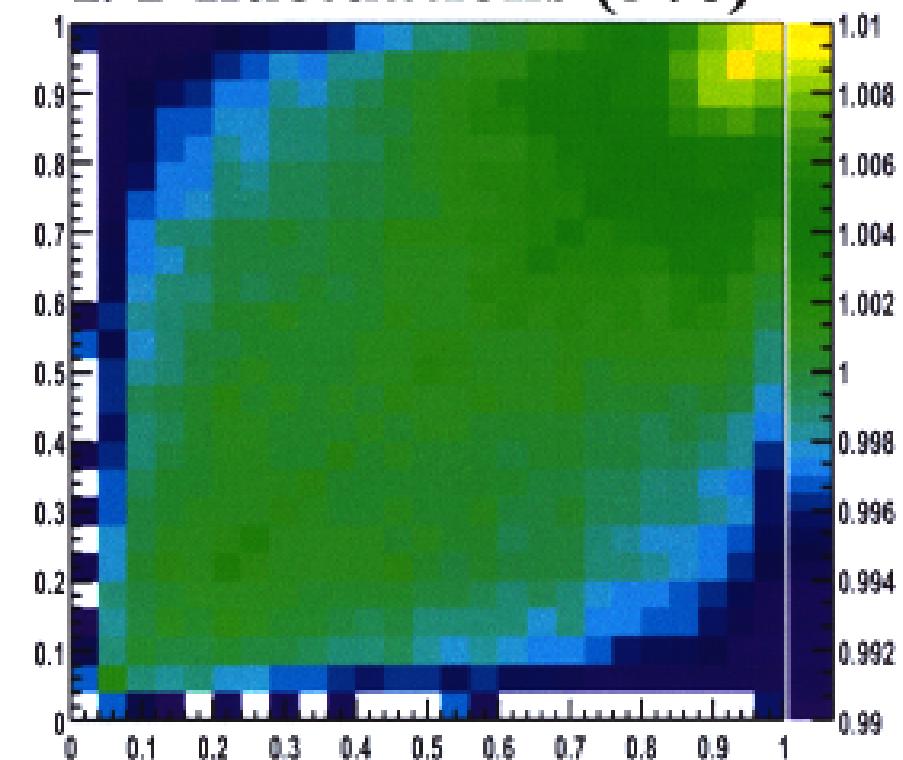


# $m_t \times m_t$ - simulation comparison

STAR Preliminary Data



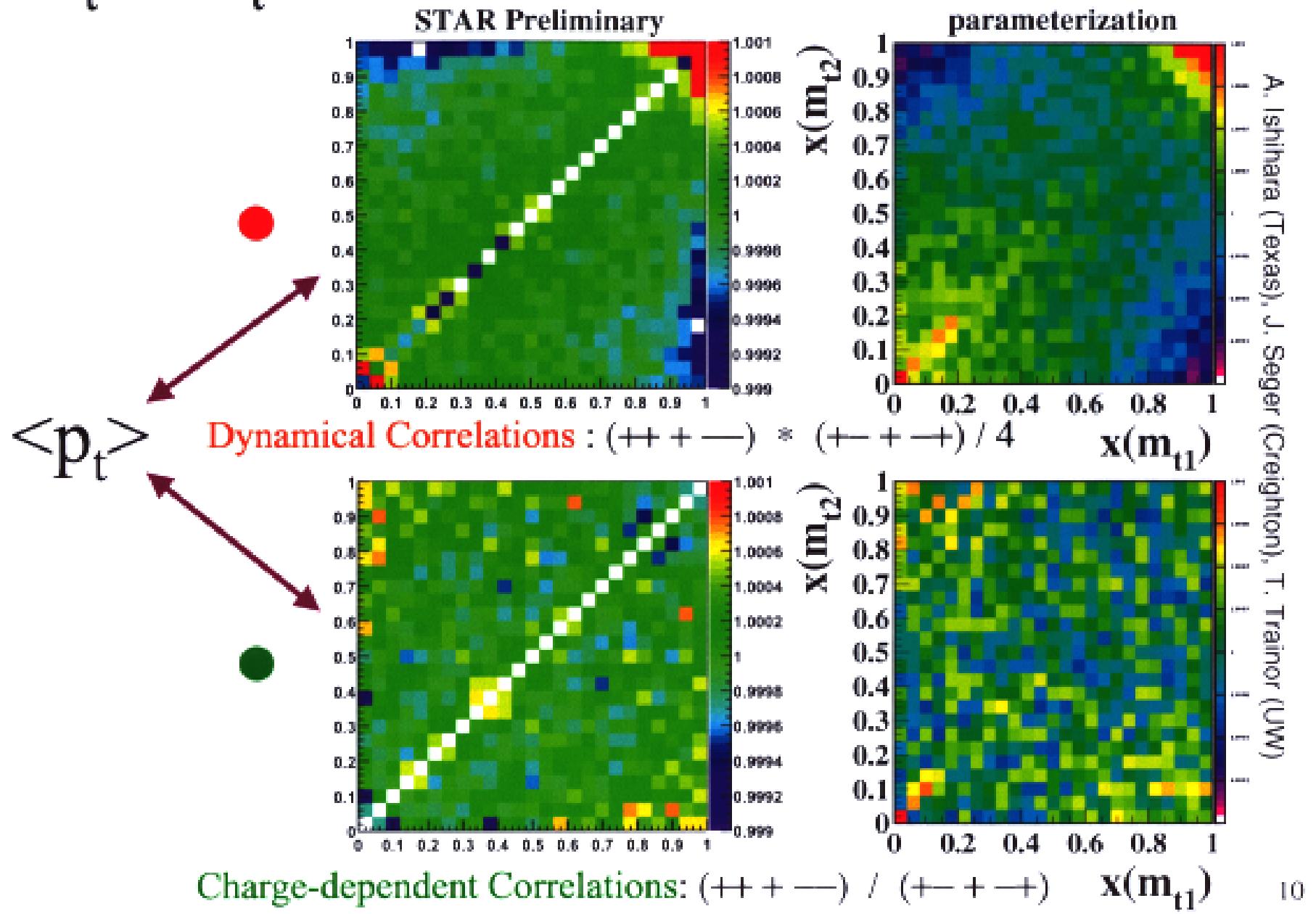
*mevsim\** Monte Carlo:  
1/T fluctuations (5%)



- Data consistent with **dynamical-fluctuations** simulation

\*L. Ray (UTA) and R. Longacre (BNL)

# $m_t \times m_t$ Correlations - DF and CD Fits

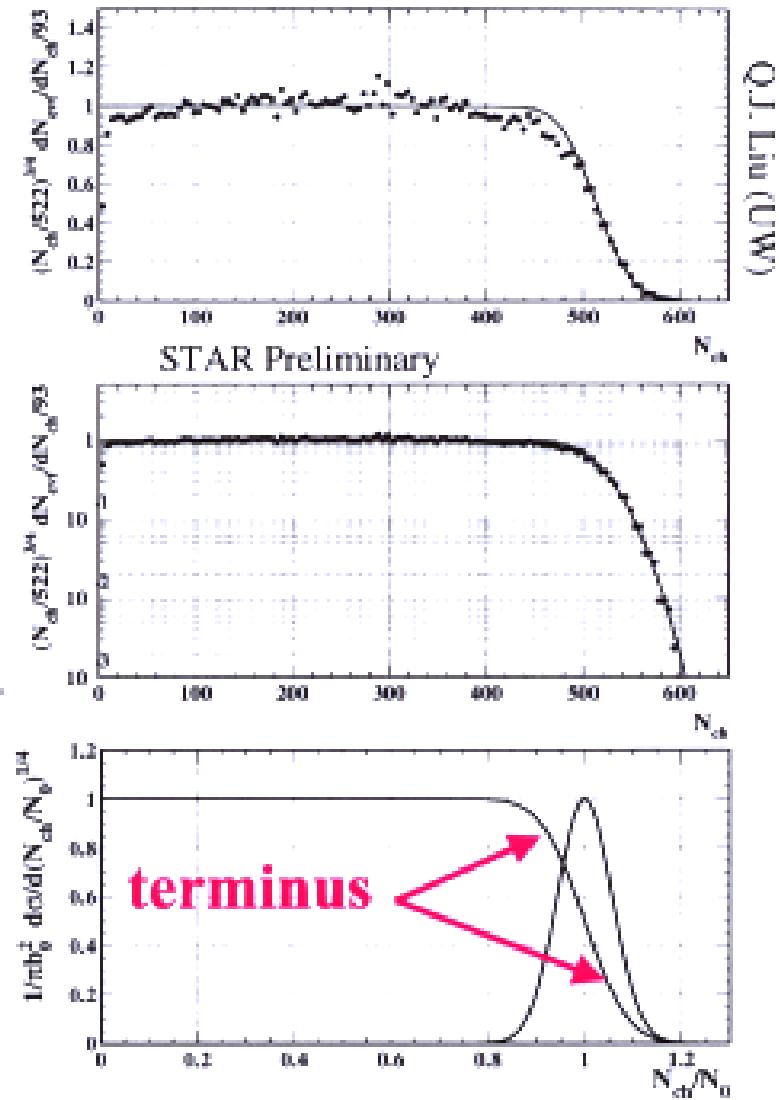


# $N_+, N_-$ Fluctuations and $d\sigma/dN_{ch}$

- $d\sigma/dN_{ch}$  distribution *transformed to*  $N_{ch}^{1/4}$  has a simple structure with a **terminus** shape determined by fluctuations
- *erf* used to model the *terminus*
- $\sigma_\Sigma^2$ ,  $\sigma_+^2$  and  $\sigma_-^2$  obtained from *erf*
- $\sigma_\Delta^2$  extracted from charge-ratio data
- Sum and difference variances are:

$$\sigma_\Sigma^2 = \sigma_+^2 + \sigma_-^2 + 2\sigma_{+-}^2$$

$$\sigma_\Delta^2 = \sigma_+^2 + \sigma_-^2 - 2\sigma_{+-}^2$$



# $N_+, N_-$ Fluctuations - Predictions

$$\sigma_{\Sigma}^2 = N_{ch} + \sigma_V^2 + \sigma_R^2 - \sigma_S^2$$

$$\sigma_{\Delta}^2 = N_{ch} - \sigma_R^2 - \sigma_S^2$$

$$\sigma_V^2 - 2\sigma_S^2 = \sigma_{\Sigma}^2 + \sigma_{\Delta}^2 - 2N_{ch}$$

$$\sigma_R^2 + \sigma_S^2 = N_{ch} - \sigma_{\Delta}^2$$

- *Volume/trigger fluctuations (V)*

- *increase*  $\Sigma$  fluctuations
  - *don't change*  $\Delta$  fluctuations
  - $\sigma_V^2 = 0.85N(BH), 0.40N(DS)$

BH G. Baym, H. Heiselberg, nucl-th/9905022,  
Phys. Lett., **B469** 5435 (1999)7-11

DS G.V. Danilov, E. Shuryak, nucl-th/9908027

JK1 S. Jeon, V. Koch, nucl-th/9906074, Phys.  
Rev. Lett., **83** 5435 (1999)

SRS M. Stephanov, K. Rajagopal, E. Shuryak,  
hep-ph/9903292, Phys. Rev. **D60** 114028 (1999)

JK2 S. Jeon, V. Koch, Phys. Rev. Lett. **85** (2000)  
2076-2079

AHM M. Asakawa, U. Heinz, B. Mueller, Phys.  
Rev. Lett. **85** (2000) 2072-2075

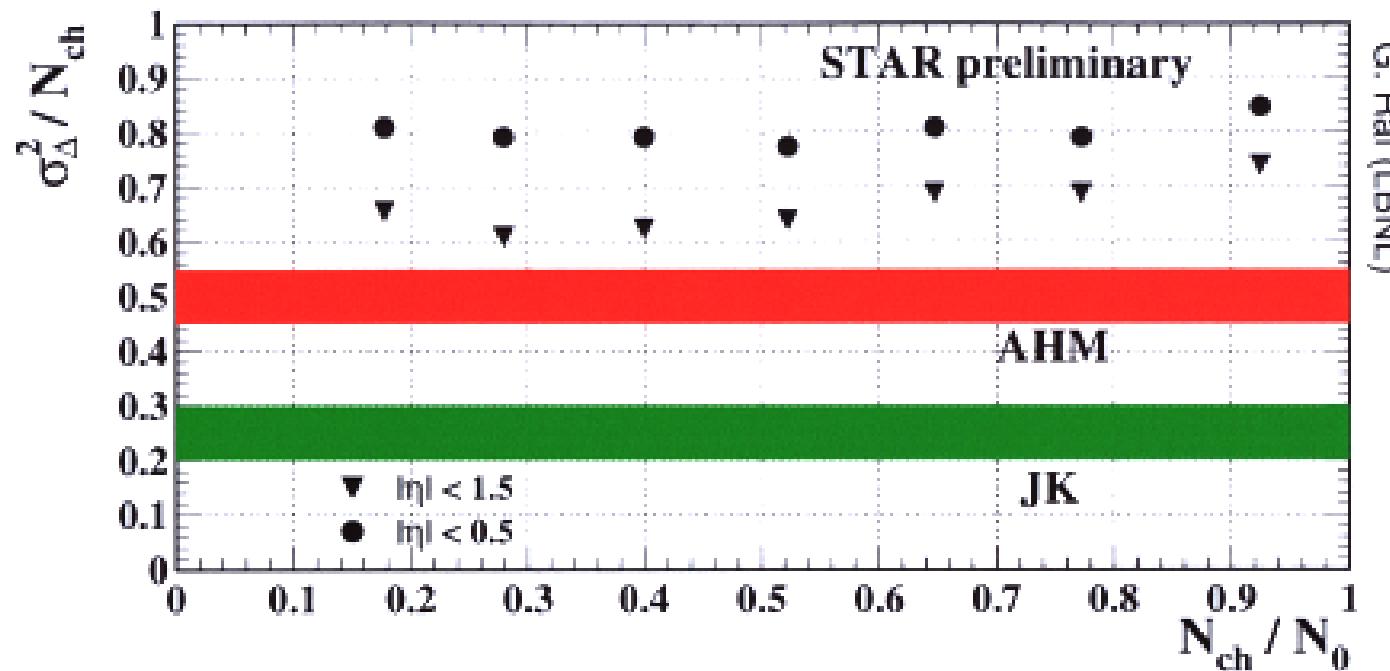
- *Resonance correlations (R)*

- *increase*  $\Sigma$  fluctuations
  - *decrease*  $\Delta$  fluctuations
  - $\sigma_R^2 = 0.3N(JK1 - \sigma_{\Delta}^2), 0.5N(SRS - \sigma_{\Sigma}^2)$

- ‘QGP’ fluctuation suppression (S)

- suppress *all* fluctuations to some extent
  - $\sigma_S^2 = 0.75N(JK2), 0.5N(AHM)$

# $N_+, N_-$ Fluctuations - Centrality Dependence



- Charge-ratio studies provide  $\sigma_{\Delta}^2$  for central events:  $0.75-0.85 N_{ch}$
- Small centrality dependence in minbias analysis
- Deviations from unity consistent with resonance correlations
- Expected dependence on  $\eta$  acceptance
- Multiplicity fluctuations: agreement between SPS\* and RHIC

\* NA49 EbyE Fluctuations poster - QM2001 session A: P082

# $N_+, N_-$ Fluctuations - Central Events

- $\sigma^2_+ = 1.50 N_+$ ,  $\sigma^2_- = 1.35 N_-$ ,  $\sigma^2_\Sigma = 2.09 N_{\text{ch}}$  [terminus variance]
- $\sigma^2_\Delta \sim 0.75 N_{\text{ch}}$  [charge-ratio]
- Experimental information is not determining
  - assume  $\sigma^2_S = 0$  and compare  $\sigma^2_R$  and  $\sigma^2_V$  predictions to data OR
  - accept predictions for  $\sigma^2_R$  and  $\sigma^2_V$  and establish constraints on  $\sigma^2_S$  from data
- Using  $\sigma^2_\Sigma = 2.09N_{\text{ch}}$  &  $\sigma^2_\Delta = 0.75N_{\text{ch}}$ 
  - Volume/trigger fluctuations (V) :  $\sigma^2_V = 0.83N_{\text{ch}} + 2\sigma^2_S$ 
    - theory:  $\sigma^2_V = 0.40N_{\text{ch}}, 0.85N_{\text{ch}}$
  - Resonance correlations (R) :  $\sigma^2_R = 0.25N_{\text{ch}} - \sigma^2_S$ 
    - theory:  $\sigma^2_R = 0.3N_{\text{ch}}, 0.5N_{\text{ch}}$
  - QGP suppression (S) :  $\sigma^2_S < 0.1N_{\text{ch}}$  (given  $\sigma^2_R, \sigma^2_V$  predictions)
    - theory:  $\sigma^2_S = 0.25N_{\text{ch}}, 0.5N_{\text{ch}}$

# EbyE Fluctuations - Summary

- *Transverse* phase-space analysis
- Charge-independent and dependent  $\langle p_t \rangle$  fluctuations
- Charge-independent and dependent correlations in  $m_t \times m_t$  distributions
  - consistent with  $\langle p_t \rangle$  results and model studies
  - *charge-dependent* correlations similar to NA49
- Multiplicity fluctuation results
  - agreement with NA49 (central)
  - $N_+/N_-$  ratio fluctuation results consistent with hadronic resonances
  - No remarkable centrality dependence
  - No substantial evidence for predicted fluctuation suppression associated with rapid hadronization from a QGP
- Much more to come from EbyE:
  - *Axial* phase-space analysis
  - High- $p_t$  correlations (minijets) [poster B:P162 (S. Chattopadhyay)]
  - QCD P,T violation [poster B:P167 (E. Finch)]
  - Flavor fluctuations (identified-particle EbyE)